AS

## MATHEMATICS

7356/2
Paper 2
Mark scheme
June 2021
Version: 1.0 Final Mark Scheme

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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## Mark scheme instructions to examiners

## General

The mark scheme for each question shows:

- the marks available for each part of the question
- the total marks available for the question
- marking instructions that indicate when marks should be awarded or withheld including the principle on which each mark is awarded. Information is included to help the examiner make his or her judgement and to delineate what is creditworthy from that not worthy of credit
- a typical solution. This response is one we expect to see frequently. However credit must be given on the basis of the marking instructions.

If a student uses a method which is not explicitly covered by the marking instructions the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

## Key to mark types

| $M$ | mark is for method |
| :--- | :--- |
| $R$ | mark is for reasoning |
| A | mark is dependent on $M$ or $m$ marks and is for accuracy |
| B | mark is independent of $M$ or $m$ marks and is for method and accuracy |
| E | mark is for explanation |
| $F$ | follow through from previous incorrect result |

## Key to mark scheme abbreviations

| CAO | correct answer only |
| :--- | :--- |
| CSO | correct solution only |
| ft | follow through from previous incorrect result |
| 'their' | indicates that credit can be given from previous incorrect result |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| sf | significant figure(s) |
| dp | decimal place(s) |

## AS/A-level Maths/Further Maths assessment objectives

| AO |  | Description |
| :---: | :---: | :---: |
| A01 | A01.1a | Select routine procedures |
|  | A01.1b | Correctly carry out routine procedures |
|  | AO1.2 | Accurately recall facts, terminology and definitions |
| AO2 | AO2.1 | Construct rigorous mathematical arguments (including proofs) |
|  | AO2.2a | Make deductions |
|  | AO2.2b | Make inferences |
|  | AO2.3 | Assess the validity of mathematical arguments |
|  | AO2.4 | Explain their reasoning |
|  | AO2.5 | Use mathematical language and notation correctly |
| AO3 | A03.1a | Translate problems in mathematical contexts into mathematical processes |
|  | A03.1b | Translate problems in non-mathematical contexts into mathematical processes |
|  | A03.2a | Interpret solutions to problems in their original context |
|  | A03.2b | Where appropriate, evaluate the accuracy and limitations of solutions to problems |
|  | AO3.3 | Translate situations in context into mathematical models |
|  | AO3.4 | Use mathematical models |
|  | A03.5a | Evaluate the outcomes of modelling in context |
|  | A03.5b | Recognise the limitations of models |
|  | A03.5c | Where appropriate, explain how to refine models |

Examiners should consistently apply the following general marking principles:

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to students showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the student to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Work erased or crossed out

Erased or crossed out work that is still legible and has not been replaced should be marked. Erased or crossed out work that has been replaced can be ignored.

## Choice

When a choice of answers and/or methods is given and the student has not clearly indicated which answer they want to be marked, mark positively, awarding marks for all of the student's best attempts. Withhold marks for final accuracy and conclusions if there are conflicting complete answers or when an incorrect solution (or part thereof) is referred to in the final answer.

| $\mathbf{Q}$ | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{1}$ | Circles correct answer | 1.1 b | B1 | $a^{a^{\frac{3}{2}}}$ |
|  |  |  |  |  |


| $\mathbf{Q}$ | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{2}$ | Ticks correct box | 2.2a | B 1 |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  | Total |  | $\mathbf{1}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 3 | Rewrites $\sqrt{x}$ as $x^{\frac{1}{2}}$ | 1.1b | B1 | $\frac{\mathrm{d} y}{\mathrm{~d} x}=x^{\frac{1}{2}}$ |
|  | Integrates their $x^{k}$ for noninteger $k$ to obtain $x^{k+1}$ | 1.1a | M1 |  |
|  | Obtains $y=\frac{2}{3} x^{\frac{3}{2}}+c$ <br> Condone no constant of integration or numerical value for c used | 1.1b | A1 |  |
|  | Total |  | 3 |  |


| $\mathbf{Q}$ | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{4 ( a )}$ | Expands, at least first term and <br> one other term correct | 1.1 a | M1 | $1+5 \times(-2 x)+\frac{5 \times 4}{2}(-2 x)^{2}$ |
|  | Expands with all terms correctly <br> simplified | 1.1 b | A1 | $=1-10 x+40 x^{2}$ |
|  | Subtotal |  | $\mathbf{2}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| 4(b) | Correctly expands $(1+5 x)^{2}$ | 1.1 a | M1 | $(1+5 x)^{2}=1+10 x+25 x^{2}$ |
|  | Obtains correct simplified <br> expression for their <br> $(1-2 x)^{5}+(1+5 x)^{2}$ | 1.1 b | A1F | $2+65 x^{2}$ |
|  | Subtotal |  |  |  |
|  |  | $\mathbf{2}$ |  |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| 4(c) | Obtains $x=0.001$ as the value <br> to use | 3.1 a | M1 | Use $x=0.001$ |
|  | Obtains 2.000065 <br> CSO | 1.1 b | A1 | $2+65 \times 0.001^{2}$ |


|  | Question Total | 6 |  |
| :--- | :--- | :--- | :--- |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 5(a) | Uses cosine rule or sine rule correctly to obtain any unknown angle or length | 1.1b | B1 |  |
|  | Uses the cosine rule to find an expression for, or the length of, AC | 1.1a | M1 | 8 cm <br> Using cosine rule $7^{2}=8^{2}+x^{2}-2 \times 8 \times x \times \cos 60$ |
|  | Deduces that $A C=5 \mathrm{~cm}$ (AWRT) <br> Condone missing or incorrect units | 2.2a | R1 | $\begin{aligned} & x=3 \text { or } 5 \\ & A C=5 \mathrm{~cm} \end{aligned}$ |
|  | Subtotal |  | 3 |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{5 ( b )}$ | States $A D=3 \mathrm{~cm}$ <br> Condone missing or incorrect <br> units | 1.1 b | B 1 | $A D=3 \mathrm{~cm}$ |
|  | Subtotal |  | $\mathbf{1}$ |  |


|  | Question Total | $\mathbf{4}$ |  |
| :--- | :--- | :--- | :--- |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 6 | Takes logs to base 5 of both sides. Condone use of any base. | 1.1a | M1 | Take logs $2 x+4=\log _{5} 9$ $2 x+4=2 \log _{5} 3$ |
|  | Writes $\log _{a} 9$ as $2 \log _{a} 3$ OE | 1.1b | B1 | $x=-2+\log _{5} 3$ |
|  | Obtains correct simplified answer <br> PI by $\mathrm{a}=-2$ and $\mathrm{b}=3$ | 1.1b | A1 |  |
|  | Total |  | 3 |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| 7(a) | States correct coordinates of $B$ <br> or $C$ <br> Or <br> States the correct x coordinates <br> of B and C | 1.1 a | M1 | $A$ is $(0,2)$ <br> $B$ is $(1,0)$ <br> $C$ is $(2,0)$ |
|  | Obtains A(0, 2), B(1, 0) and <br> C(2,0) | 1.1 b | A1 |  |
|  | Subtotal |  | $\mathbf{2}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 7(b)(i) | Integrates in two parts with limits $O$ to $B$ and $B$ to $C$ | 3.1a | M1 | $\int_{0}^{1}\left(x^{2}-3 x+2\right) \mathrm{d} x$ |
|  | Integrates quadratic function with at least one term correct | 1.1a | M1 | $=\left[\frac{1}{3} x^{3}-\frac{3}{2} x^{2}+2 x\right]_{0}^{1}$ |
|  | Integrates completely correctly | 1.1b | A1 |  |
|  | Substitutes the two sets of their limits and subtracts the $B C$ value from the $O B$ value or uses the modulus for the $B C$ value | 1.1a | M1 | $\left[\frac{1}{3} x^{3}-\frac{3}{2} x^{2}+2 x\right]_{1}^{2}$ |
|  | Completes calculation of total area convincingly to given answer. AG | 2.1 | R1 | Total area $=\frac{5}{6}-\left(-\frac{1}{6}\right)=1$ |
|  | Subtotal |  | 5 |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| 7(b)(ii) | Explains that the area between <br> B and C is treated as negative <br> (OE) | 2.3 | E1 | The calculator treats the area <br> between B and C as negative. |
|  | Subtotal |  | $\mathbf{1}$ |  |


|  | Question Total | $\mathbf{8}$ |  |
| :--- | :--- | :--- | :--- | :--- |



| $\mathbf{Q}$ | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{9 ( a )}$ | States correct factorisation | 1.1 b | B 1 | $n^{3}-n=n\left(n^{2}-1\right)$ |
|  |  |  |  | $=n(n-1)(n+1)$ |
|  | Subtotal |  | $\mathbf{1}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| 9(b) | States that $(n-1), n,(n+1)$ are <br> 3 consecutive integers. <br> Or <br> States that all integers are either <br> a multiple of 3 or 1 more or less <br> than a multiple of 3 | 3.1 a | E 1 | $(n-1) n(n+1)$ is the product of <br> three consecutive integers <br> So one must be a multiple of 3 |
| And at least one must be a multiple <br> of 2 |  |  |  |  |
| Deduces that one of these <br> factors must be a multiple of 3 <br> (PI) <br> Or <br> Deduces that one of these <br> factors must be a multiple of 2. <br> Condone 'even' for implied <br> multiple of 2. | 2.2 a | E1 | So the product has factors of <br> 2 and 3, |  |
| States that at least one must be |  |  |  |  |
| a multiple of 2 (even), one must <br> be a multiple of 3 and draws <br> correct conclusion. | 2.1 | R 1 | so is a multiple of $2 \times 3=6$ |  |
|  |  | 3 |  |  |


|  | Question Total | $\mathbf{4}$ |  |
| :--- | ---: | :--- | :--- |


| $\mathbf{Q}$ | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{1 0 ( a )}$ | Uses side of box is $30-2 x$ | 3.1 b | M 1 | $C=x(30-2 x)^{2}$ <br> $=x\left(900-120 x+4 x^{2}\right)$ |
|  | Identifies the three dimensions <br> then expands correctly to obtain <br> answer AG | 2.1 | R 1 | $C=900 x-120 x^{2}+4 x^{3}$ |
|  | Subtotal |  | $\mathbf{2}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 10(b) | Differentiates, at least one term correct | 1.1a | M1 | $\frac{\mathrm{d} C}{\mathrm{~d} x}=900-240 x+12 x^{2}$ |
|  | Obtains correct derivative | 1.1b | A1 | For maximum $\frac{\mathrm{d} C}{\mathrm{~d} x}=$ |
|  | Explains $\frac{\mathrm{d} C}{\mathrm{~d} x}$ must be 0 for turning point (or maximum) | 2.4 | E1 | $x=5 \text { or } 15$ <br> however $x<15$ therefore $x=5$ |
|  | Equates their derivative to 0 and solves to find a value of $x<15$ | 1.1a | M1 | Negative when $x=5$ |
|  | Obtains $x=5$ | 1.1b | A1 |  |
|  | Justifies $x=5$ is the maximum | 2.1 | R1 |  |
|  | States maximum capacity CAO <br> Condone incorrect or missing units | 3.2a | A1 |  |
|  | Subtotal |  | 7 |  |


|  | Question Total | 9 |  |
| :--- | :--- | :--- | :--- |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{1 1 ( a ) ( i )}$ | Writes down the equation of the <br> circle in any correct form | 1.1 b | B1 | Circle equation is <br> $(x-0)^{2}+(y-10)^{2}=(\sqrt{ } 20)^{2}$ |
|  | Substitutes $m x$ for $y$ | 1.1 a | M1 | $x^{2}+y^{2}-20 y+100=20$ <br> $x^{2}+y^{2}-20 y+80=0$ <br> Substitute $y=m x$ |
|  | Simplifies to the given quadratic <br> AG | 2.1 | R1 | $x^{2}+m^{2} x^{2}-20 m x+80=0$ <br> $\left(1+m^{2}\right) x^{2}-20 m x+80=0$ |
|  | Subtotal |  | $\mathbf{3}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| 11(a)(ii) | Uses the discriminant of the <br> given equation from (a)(i) | 3.1 a | M1 | Using $b^{2}=4 a c$ <br> $400 m^{2}=4 \times\left(1+m^{2}\right) \times 80$ |
|  | Obtains a correct equation in $m$ | 1.1 b | A 1 | $5 m^{2}=4 \times\left(1+m^{2}\right)$ <br> $m^{2}=4$ |
|  | Obtains $m= \pm 2$ | 1.1 b | A 1 | $\mathrm{~m}= \pm 2$ |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 11(b) | Uses one of their $m$ values from (a)(ii) | 3.1a | M1 | Using $m=2$ in equation from (a) $\begin{gathered} 5 x^{2}-40 x+80=0 \\ x=4 \text { giving } y=8 \end{gathered}$ <br> Using $m=-2$ in equation from (a) $\begin{aligned} & 5 x^{2}+40 x+80=0 \\ & x=-4 \text { giving } y=8 \end{aligned}$ <br> So (4, 8) and (-4, 8) |
|  | Obtains one correct $x$ value | 1.1b | A1 |  |
|  | Uses line equation to calculate $y$ value | 1.1a | M1 |  |
|  | Obtains two correct sets of coordinates | 1.1b | A1 |  |
|  | Subtotal |  | 4 |  |


| $\mathbf{Q}$ | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| 12 | Circles the correct answer | 2.2 b | B1 | Systematic |
|  | Total |  | 1 |  |


| $\mathbf{Q}$ | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| 13 | Circles the correct answer | 1.1 b | B1 | 0.58 |
|  | Total |  |  | 1 |
|  |  |  |  |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 4 ( a )}$ | Uses np to find $\mu$ <br> PI by 4.8 | 1.1 a | M 1 | $\mu=\mathrm{np}$ <br> $=16 \times 0.3$ |
|  | Obtains the correct probability <br> (AWRT 0.45) | 3.4 | A 1 | $=4.8$ <br> $\mathrm{P}(T \leq 4.8)=\mathrm{P}(T \leq 4)$ |
|  | Subtotal |  | $\mathbf{2}$ | $=0.4499$ |


| $\mathbf{Q}$ | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 4 ( b )}$ | Finds the correct variance <br> (CAO) | 1.1 b | B1 | Variance $=16 \times 0.3 \times 0.7$ <br> $=3.36$ |
|  | Subtotal |  | $\mathbf{1}$ |  |


|  | Question Total | 3 |  |
| :--- | :--- | :--- | :--- |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| 15(a)(i) | Deduces the correct letter | 2.2 a | B1 | F |
|  | Subtotal |  |  | 1 |
|  |  |  |  |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| 15(a)(ii) | States an appropriate action to <br> deal with the error | 2.4 | E1 | Remove the point from the set of <br> data |
|  | Subtotal |  | $\mathbf{1}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| 15(b) | Indicates somewhere in their <br> response that the scatter <br> diagram does not imply <br> causality (ISW) | 2.4 | E1 | The claim is invalid because <br> correlation does not imply <br> causality. |
| Or <br> Identifies any counter example <br> from the data and concludes | Subtotal |  | $\mathbf{1}$ |  |
|  |  |  |  |  |


|  | Question Total |  | 3 |  |
| :--- | :--- | :--- | :--- | :--- |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 16(a) | Obtains either 171 or 124 (AWRT) | 1.1a | M1 | $\text { Mean }_{2002}=171$ |
|  | Subtracts means to obtain correct difference (AWRT) Or Expresses as a $27 \%$ reduction (AWRT) | 1.1b | A1 | Reduction $=171-124=47$ |
|  | Subtotal |  | 2 |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 6 ( b )}$ | Disagrees with the statement <br> and refers to the small number <br> (1 of each) of these types of car <br> in the data set for 2016 not <br> being able to cause such a fall <br> in the mean (OE) | 2.4 | E1 | Disagree with the statement as <br> there are very few cars of these <br> types in the LDS in 2016, so they <br> alone cannot have caused this <br> reduction in the mean emissions |
|  | Subtotal |  | $\mathbf{1}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 6 ( c ) ( i )}$ | Shows that the total sample size <br> is 2359 and indicates this is <br> different to the total size of the <br> LDS (3827). <br> Implied by mention of 1468 <br> missing/extra <br> or <br> Total sample size is less than <br> 3827 | 2.4 | E1 | The claim is being made because |
|  | Subtotal |  | $\mathbf{1}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 6 ( c ) ( i i ) ~}$ | Gives an indication that the LDS <br> also has other categories | 2.4 | E1 | The claim is incorrect because the <br> LDS also has a 'Company' car <br> category |
|  | Subtotal |  | $\mathbf{1}$ |  |


|  | Question Total |  | 5 |  |
| :--- | :--- | :--- | :--- | :--- |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| 17(a)(i) | States correct answer (ACF) | 1.1 b | B 1 | $\mathrm{P}(A)=\frac{100}{200}$ |
| $=0.5$ |  |  |  |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 7 ( a )}$ (ii) | States correct answer (ACF) | 1.1 b | B1 | Find $\mathrm{P}\left(A^{\prime} \cap B\right)=\frac{20}{200}=0.1$ |
|  | Subtotal |  | $\mathbf{1}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 17(a)(iii) | Uses correct formula for $\mathrm{P}(A \cup B)$ with 'their' $\mathrm{P}(A), \mathrm{P}(B)$ and $\mathrm{P}(A \cap B)(\neq 0)$ <br> ( Pl by correct answer) <br> Or <br> Counting from the table $\frac{12+8+10+50+30+10}{200}$ <br> Condone double-counting the 10 for $A \cap B$ for this mark. | 3.1a | M1 | $\begin{aligned} & \mathrm{P}(B)=\frac{30}{200}=0.15 \\ & \mathrm{P}(A \cap B)=\frac{10}{200}=0.05 \\ & \begin{aligned} \mathrm{P}(A \cup B) & =\mathrm{P}(A)+\mathrm{P}(B)-\mathrm{P}(A \cap B) \\ \mathrm{P}(A \cup B) & =0.5+0.15-0.05 \\ & =0.6 \end{aligned} \end{aligned}$ |
|  | Obtains correct answer. (ACF) | 1.1b | A1 |  |
|  | Subtotal |  | 2 |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 7 ( b )}$ | Calculates $\mathrm{P}(A) \times \mathrm{P}(B)$ for 'their' <br> $\mathrm{P}(A)$ and $\mathrm{P}(B)$ | 3.1 a | M 1 | $\mathrm{P}(A) \times \mathrm{P}(B)=0.5 \times 0.15$ <br> $=0.075$ |
|  | Compares to 'their' $\mathrm{P}(A \cap B)$ <br> (providing $\mathrm{P}(A \cap B) \neq 0)$ and <br> deduces that the events are not <br> independent | 2.2 a | A1F | As $\mathrm{P}(A \cap B) \neq \mathrm{P}(A) \times \mathrm{P}(B)$ <br> Events $A$ and $B$ are not <br> independent |
|  | Subtotal |  | $\mathbf{2}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 7 ( c )}$ | States any two events which are <br> mutually exclusive, but must be <br> different to events $A$ and $B$ | 1.1 b | B1 | Event 1 is the event the property <br> has 1 toilet <br> Event 2 is the event the property |
| 2 from terraced / semi - |  |  |  |  |
| detached /apartment |  |  |  |  |
| Or toilets <br> 1 toilet and 3 toilets <br> Or <br> apartment and 3 toilets | Subtotal |  | $\mathbf{1}$ |  |
|  |  |  |  |  |


|  | Question Total | 7 |  |
| :--- | :--- | :--- | :--- | :--- |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 8 ( a )}$ | Explains why this test is a one- <br> tailed test. Must be in context. <br> Condone explanation using <br> 'number of linked to increase | 3.2 a | E1 | If the campaign is effective, then <br> the proportion of under 30s visitors <br> will be greater than 14\%. So, a <br> one-tailed test is required. |
|  | Subtotal |  | $\mathbf{1}$ |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :---: | :---: | :---: | :---: |
| 18(b) | States both hypotheses correctly for a one-tailed test. Accept population proportion for p. Accept $14 \%$, but not $x=$ or $\bar{x}=$ or $\mu=$ | 2.5 | B1 | $X$ is 'No of under 30's visitors to the website' $\begin{aligned} & H_{0}: p=0.14 \\ & H_{1}: p>0.14 \end{aligned}$ |
|  | States model used (PI by 0.016(5), 0.0071(5), 0.035, $0.0029,0.0093$ ) (AWRT) | 1.1a | M1 | Under $\mathrm{H}_{0}: X \sim \mathrm{~B}(60,0.14)$ $\begin{aligned} \mathrm{P}(X \geq 15) & =1-\mathrm{P}(X \leq 14) \\ & =1-0.98351 \ldots \end{aligned}$ |
|  | Evaluates using calculator $=$ 0.016(5) (AWRT) (condone 0.0071 (5) for A1) | 1.1b | A1 | $\begin{aligned} &=0.0165 \\ & \text { As } 0.0165<0.05 \end{aligned}$ |
|  | Compares 0.016(5) to 0.05 and rejects $\mathrm{H}_{0}$. (PI)(CSO) <br> No ft here. Must see clear comparison (inequality or diagram) | 3.5a | A1 | Reject $\mathrm{H}_{0}$ <br> There is sufficient evidence to suggest that the advertising campaign has been effective. |
|  | Concludes correctly in context CSO ‘sufficient evidence’ OE required. Only award for full complete correct solution. | 3.2a | R1 |  |
|  | Subtotal |  | 5 |  |


| Q | Marking instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 8 ( c )}$ | Recalls that the sample would <br> need to be Random. Accept <br> 'not biased' OE | 1.2 | E1 | The sample would need to be a <br> Random sample |
|  | Subtotal |  | $\mathbf{1}$ |  |

