AS

## MATHEMATICS

7356/2
Paper 2
Mark scheme
June 2020
Version: 1.0 Final Mark Scheme

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

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## Mark scheme instructions to examiners

## General

The mark scheme for each question shows:

- the marks available for each part of the question
- the total marks available for the question
- marking instructions that indicate when marks should be awarded or withheld including the principle on which each mark is awarded. Information is included to help the examiner make his or her judgement and to delineate what is creditworthy from that not worthy of credit
- a typical solution. This response is one we expect to see frequently. However credit must be given on the basis of the marking instructions.

If a student uses a method which is not explicitly covered by the marking instructions the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

## Key to mark types

| M | mark is for method |
| :--- | :--- |
| $R$ | mark is for reasoning |
| A | mark is dependent on M marks and is for accuracy |
| B | mark is independent of M marks and is for method and accuracy |
| E | mark is for explanation |
| F | follow through from previous incorrect result |

## Key to mark scheme abbreviations

| CAO | correct answer only |
| :--- | :--- |
| CSO | correct solution only |
| ft | follow through from previous incorrect result |
| 'their' | Indicates that credit can be given from previous incorrect result |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| NMS | no method shown |
| PI | possibly implied |
| sf | significant figure(s) |
| dp | decimal place(s) |

## AS/A-level Maths/Further Maths assessment objectives

| AO |  | Description |
| :---: | :---: | :---: |
| A01 | AO1.1a | Select routine procedures |
|  | A01.1b | Correctly carry out routine procedures |
|  | AO1.2 | Accurately recall facts, terminology and definitions |
| AO2 | AO2.1 | Construct rigorous mathematical arguments (including proofs) |
|  | AO2.2a | Make deductions |
|  | AO2.2b | Make inferences |
|  | AO2.3 | Assess the validity of mathematical arguments |
|  | AO2.4 | Explain their reasoning |
|  | AO2.5 | Use mathematical language and notation correctly |
| AO3 | A03.1a | Translate problems in mathematical contexts into mathematical processes |
|  | A03.1b | Translate problems in non-mathematical contexts into mathematical processes |
|  | AO3.2a | Interpret solutions to problems in their original context |
|  | A03.2b | Where appropriate, evaluate the accuracy and limitations of solutions to problems |
|  | A03.3 | Translate situations in context into mathematical models |
|  | A03.4 | Use mathematical models |
|  | A03.5a | Evaluate the outcomes of modelling in context |
|  | A03.5b | Recognise the limitations of models |
|  | AO3.5c | Where appropriate, explain how to refine models |

Examiners should consistently apply the following general marking principles

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to students showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the student to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Work erased or crossed out

Erased or crossed out work that is still legible and has not been replaced should be marked. Erased or crossed out work that has been replaced can be ignored.

## Choice

When a choice of answers and/or methods is given and the student has not clearly indicated which answer they want to be marked, mark positively, awarding marks for all of the student's best attempts. Withhold marks for final accuracy and conclusions if there are conflicting complete answers or when an incorrect solution (or part thereof) is referred to in the final answer.

| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{1}$ | Circles correct answer | 1.1 b | B 1 | $\frac{1}{\sqrt[5]{e^{2}}}$ |
|  |  |  |  |  |


| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{2}$ | Ticks correct box | 1.1 b | B 1 | $-1<y<0$ |
|  |  | Total |  | $\mathbf{1}$ |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :---: |
| 3 | Differentiates once, at least one <br> term correct | 1.1a | M1 | $\frac{d y}{d x}=12 x^{3}-\frac{2}{x^{2}}-\frac{1}{4}$ |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
|  | Uses substitution $\cos ^{2} x=1-\sin ^{2} x$ in any form | 1.2 | B1 | $9 \sin ^{2} x-6 \sin x+\left(1-\sin ^{2} x\right)=0$ |
|  | Solves 'their' quadratic to obtain two values for $\sin x$ | 1.1a | M1 | $(4 \sin x-1)(2 \sin x-1)$ |
|  | Finds two correct solutions for $x$ | 1.1b | A1 | $\sin x=1 / 2$ |
|  | Finds all four solutions for $x$ and no extras (condone 14.5, 165.5 AWRT) | 1.1b | A1 |  |
|  | Total |  | 4 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 5 | Chooses $x^{3}$ term (PI) | 1.1b | B1 |  |
|  | Uses correct coefficient formula, allow use of either ${ }^{7} \mathrm{C}_{3}$ or ${ }^{7} \mathrm{C}_{4}$ (OE) | 1.1a | M1 | $-15120 x^{3}$ |
|  | Obtains -15120 or 22680 as the value of the coefficient (ignore any power of $x$ if included as part of the coefficient) | 1.1b | A1F | Joseph has the right number but the wrong sign |
|  | Obtains -15120 and explains how the error could have occurred or what the error is | 2.4 | R1 |  |
|  | Total |  | 4 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 6(a) | Completes a square correctly once OE <br> (PI by one correct coordinate of the centre) | 1.1a | M1 | $\begin{gathered} x^{2}+10 x+25+y^{2}-4 y+4-100=0 \\ (x+5)^{2}+(y-2)^{2}=100 \\ \text { Centre }=(-5,2) \end{gathered}$ |
|  | Obtains correct centre | 1.1b | A1 |  |
|  | Subtotal |  | 2 |  |
| 6(b) | Finds correct gradient from 'their' centre from (a) to the point $(1,10)$ | 1.1b | B1F | Gradient from $(-5,2)$ to $(1,10)$ is $\frac{8}{6}$ |
|  | Uses perpendicular gradient property for 'their' gradient | 1.1a | M1 | So perpendicular gradient is $-\frac{3}{4}$ $y-10=-\frac{3}{4}(x-1)$ |
|  | Finds 'their' equation of the line based on 'their' perpendicular gradient. <br> Finding c $=10.75$ (OE) is sufficient for M1 | 1.1a | M1 | $\begin{gathered} 4 y-40=-3 x+3 \\ 3 x+4 y-43=0 \end{gathered}$ |
|  | Rearranges "their" equation of the line into form $a x+b y+c=0$ <br> (FT 'their' centre of the circle only) | 1.1b | A1F |  |
|  | Subtotal |  | 4 |  |
|  | Question Total |  | 6 |  |


| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{7 y y y y} \mathbf{7}$ | Multiplies by ratio of populations in <br> 1989 and 2019 | 3.1 b | M1 | 6 million $\times \frac{6 \text { million }}{3.6 \text { million }}$ |
|  | Obtains correct estimated population | 1.1 b | A1 | $=10$ million |


| Q | Marking Instructions | AO | Marks | Typical solution |
| :---: | :--- | :---: | :---: | :---: |
| 8(a) | Uses rules of indices to express <br> $2^{(2 x+3)}$ in terms of $y$ <br> or <br> $16^{x}$ in terms of $y$, must see an <br> intermediary step, either $\left(2^{4}\right)^{x}$ or <br> $\left(4^{2}\right)^{x}$, not just $16^{x}=\left(2^{2 x}\right)^{2}$ | 1.1 a | M1 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 9(a)(i) | Integrates to obtain terms in $x^{2}$ and $x^{4}$ | 1.1a | M1 | $2 x^{2}-\frac{x^{4}}{4}+c$ |
|  | Obtains fully correct integral (ISW) Condone omission of $+c$ | 1.1b | A1 |  |
|  | Subtotal |  | 2 |  |
| 9(a)(ii) | Obtains answer of 0 <br> $n b$ correct answer can be obtained directly from calculator, if working shown then CSO | 1.1b | B1 | 0 |
|  | Subtotal |  | 1 |  |
| 9(b) | Shows curve with three zeros with correct orientation | 1.1b | B1 |  <br> The area between -2 and 0 lies below the axis so its integral has a negative value |
|  | Explains that the integral for the area below the axis has a negative value (PI) <br> (Allow even if the graph is incorrectly drawn or omitted) | 2.4 | E1 |  |
|  | Subtotal |  | 2 |  |
| 9(c) | Uses $2 \times \int_{0}^{2} 4 x-x^{3} d x$ (OE) Or <br> Obtains values of 4 , and -4 or 4 from two separate integrals | 1.1a | M1 | $\begin{gathered} 2 \times \int_{0}^{2} 4 x-x^{3} d x \\ 2\left[2 x^{2}-\frac{x^{4}}{4}\right]_{0}^{2} \\ =8 \end{gathered}$ |
|  | Obtains correct area | 1.1b | A1 |  |
|  | Subtotal |  | 2 |  |
|  | Question Total |  | 7 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 10(a) | States $\frac{d y}{d x}=0$ at a turning point OE | 2.4 | E1 | At a turning point $\frac{d y}{d x}=0$$3 x^{2}-12 x+c=0$ |
|  | Substitutes $x=-1$ into $\frac{d y}{d x}=0$ | 3.1a | M1 |  |
|  | Obtains correct value for $c$ | 1.1b | A1 | Integrate to find $y$ |
|  | Obtains $x=5$ at other turning point | 1.1b | A1 |  |
|  | Integrates to find $y$, at least one term correct and substitutes point $(-1,1)$ into their integrated expression to find 'their' $k$ | 3.1a | M1 | $\frac{d y}{d x}=0 \text { gives } x=-1 \text { and } x=5$ |
|  | Obtains correct $y$ coordinate | 1.1b | A1 | $y=-107$ |
|  |  |  |  | $(5,-107)$ |
|  | Subtotal |  | 6 |  |
| 10(b) | Obtains lower inequality condone inclusion of equality | 1.1b | B1 | $x<-1$ and $x>5$ |
|  | Obtains upper inequality condone inclusion of equality | 1.1b | B1 |  |
|  | Subtotal |  | 2 |  |
|  | Question Total |  | 8 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :---: |
| 11(a)(i) | Substitutes $y=0$ to give a <br> quadratic equation (PI) | 3.1 b | M1 | $0=-0.0125 x^{2}+0.5 x-2.55$ |
|  | Solves quadratic equation | 1.1 b | M1 | $x^{2}-40 x+204=0$ |
| $(x-6)(x-34)$ |  |  |  |  |


| 11(c) | Substitutes $11+a$ into equation to find $y$. | 3.1b | M1 | $\text { Using } x=17, y=2.3375$ <br> I have assumed the jet of water has no size <br> $2.3375>2.3$ so passes over the wall |
| :---: | :---: | :---: | :---: | :---: |
|  | Explains a limitation of the model eg that the model assumes that jet has no size or a size less than 3.75 cm or <br> Wall has no width or has some width <br> or <br> No air resistance | 3.5b | E1 |  |
|  | Compares correct value with 2.3 to infer that jet passes over wall / fails to pass over the wall. Inference must be consistent with stated assumption. <br> Condone a valid comparison if no assumption given | 2.2b | R1 |  |
|  | Subtotal |  | 3 |  |
|  | Question Total |  | 11 |  |


| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| 12 | Circles correct answer | 2.2 a | B1 | A |
|  |  | Total |  | 1 |


| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 3}$ | Circles correct answer | 1.1 b | B1 | 72 |
|  |  | Total |  | $\mathbf{1}$ |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 14(a) | Explains clearly that the sample is likely to be biased (OE) <br> Do not accept "the sample is not random" alone. <br> Accept "this method does not guarantee to get an employee or opinions from each or other store(s)" (OE) <br> Accept "people from same large store may have similar opinions" (OE) | 2.4 | E1 | Likely to be a biased sample |
|  | Subtotal |  | 1 |  |
| 14(b) | Expresses the idea that method $B$ ensures that there is representation from every store (OE) <br> Method B gives every employee the opportunity of being chosen (OE) <br> Do not accept references to time | 2.4 | E1 | It guarantees to get responses from each store |
|  | Subtotal |  | 1 |  |
| 14(c)(i) | States Systematic (sampling) (CAO) | 1.2 | B1 | Systematic sampling |
|  | Subtotal |  | 1 |  |
| 14(c)(ii) | Explains clearly, in context, the idea that all samples of size 100 are not possible to be chosen using this method so the method is not random. <br> Do not accept each person is not equally likely to be selected. | 2.4 | E1 | Not all subsets of employees of size 100 are possible, so each sample of size 100 is not equally likely to be selected, so not random. |
|  | Subtotal |  | 1 |  |
|  | Question Total |  | 4 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 15(a) | States (AWRT) 22.9 Condone (AWRT) 24.1 | 1.1b | B1 | 22.9 |
|  | Subtotal |  | 1 |  |
| 15(b) | Explains or shows how 145.8 is generated from the two separate means or Explains that we do not know that the sample sizes are the same for the two years. | 2.4 | E1 | $(171.2+120.4) \div 2=145.8$ <br> However, the sample size for 2016 is larger so the claim is incorrect |
|  | Explains that the sample size for 2016 is larger than 2002 | 2.4 | E1 |  |
|  | Subtotal |  | 2 |  |
|  | Question Total |  | 3 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 16(a)(i) | Finds $\mathrm{P}(X=8)$ correctly AWRT 0.207 | 3.4 | B1 | 0.207 |
|  | Subtotal |  | 1 |  |
| 16(a)(ii) | Finds $\mathrm{P}(X \leq 11)-\mathrm{P}(X \leq 6)$. <br> Must be two terms subtracted with at least one term correct Or Terms for $\mathrm{P}(X=7,8,9,10,11)$ added, at most one error | 1.1a | M1 | $\begin{aligned} & \mathrm{P}(X \leq 11)-\mathrm{P}(X \leq 6) \\ & =0.96020841-0.1501401 \\ & =0.810 \end{aligned}$ |
|  | Obtains correct probability (AWRT 0.81) | 1.16 | A1 |  |
|  | Subtotal |  | 2 |  |
| 16(b) | States one clear assumption in context linked to independence or the constant probability of success. <br> Do not accept a fixed number of trials or she either fails or does not fail or the probability is 0.6 . | 3.5b | E1 | Being able to solve one puzzle is independent of being able to solve any other puzzle |
|  | Subtotal |  | 1 |  |
|  | Question Total |  | 4 |  |



| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 18(a) | Finds the sum of two or more products each term in the products having denominators of 12 and 11 | 1.1a | M1 | $\begin{aligned} \mathrm{P}(\text { one blue }) & =\frac{7}{12} \times \frac{5}{11}+\frac{5}{12} \times \frac{7}{11} \\ & =\frac{35}{66} \end{aligned}$ |
|  | Obtains $\frac{35}{66} \mathrm{OE}$ <br> (accept 0.53 or better) | 1.1b | A1 |  |
|  | Subtotal |  | 2 |  |
| 18(b) | Uses correct denominator ( $12 \times 10$ ) at least once | 1.1b | B1 | P(Red from Bag B)$\begin{aligned} & =\frac{8}{12} \times \frac{6}{10}+\frac{4}{12} \times \frac{7}{10} \\ & =\frac{19}{30} \end{aligned}$ |
|  | Uses correct numerator in two or three termed expression $(8 \times 6)+(4 \times 7)$ <br> or $(7 \times 6)+(4 \times 7)+(1 \times 6)$ (OE) | 1.1a | M1 |  |
|  | Obtains $\frac{19}{30}$ OE <br> (accept 0.63 or better) | 1.1b | A1 |  |
|  | Subtotal |  | 3 |  |
|  | Question Total |  | 5 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 19 | States both hypotheses correctly for a two-tailed test. Accept population proportion for $p$. Accept 15\%, but not ' $x=$ ' or ' $\bar{x}=$ ' or ' $\mu=$ ' | 2.5 | B1 | $X$ is 'Number of residents who buy Local News' $\mathrm{H}_{0}: p=0.15$ |
|  | States model used (PI by 0.046, $0.032,0.014,0.112$ ) (AWRT) | 1.1a | M1 | Under $\mathrm{H}_{0}: X \sim \mathrm{~B}(50,0.15)$ |
|  | Evaluates $\mathrm{P}(X \leq 3)=0.046(\mathrm{PI})$ (condone 0.014 for A1) | 1.1b | A1 | $\mathrm{P}(X \leq 3)=0.04604657$ |
|  | Compares 0.046 or 0.014 with 0.025 . | 3.5a | M1 | Accept $\mathrm{H}_{0}$ |
|  | Must see clear comparison (inequality or diagram) |  |  | There is insufficient evidence to suggest that the proportion of residents buying 'Local News' has changed. |
|  | Infers $\mathrm{H}_{0}$ is not rejected (PI)(CSO)(OE) | 2.2b | A1 |  |
|  | Concludes correctly in context CSO 'insufficient evidence' OE required. Only award for full complete correct solution. | 3.2a | R1 |  |
|  | Total |  | 6 |  |


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