



Additional Assessment Materials

Summer 2021

Pearson Edexcel GCE in Mathematics

9MA0 (Public release version)

Resource Set 1: Topic 7

Differentiation (Test 2)

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Additional Assessment Materials, Summer 2021

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General guidance to Additional Assessment Materials for use in 2021

Context

- Additional Assessment Materials are being produced for GCSE, AS and A levels (with the exception of Art and Design).
- The Additional Assessment Materials presented in this booklet are an optional part of the range of evidence teachers may use when deciding on a candidate's grade.
- 2021 Additional Assessment Materials have been drawn from previous examination materials, namely past papers.
- Additional Assessment Materials have come from past papers both published (those materials available publicly) and unpublished (those currently under padlock to our centres) presented in a different format to allow teachers to adapt them for use with candidate.

Purpose

- The purpose of this resource to provide qualification-specific sets/groups of questions covering the knowledge, skills and understanding relevant to this Pearson qualification.
- This document should be used in conjunction with the mapping guidance which will map content and/or skills covered within each set of questions.
- These materials are only intended to support the summer 2021 series.

1. Given $y = x(2x + 1)^4$, show that

$$\frac{dy}{dx} = (2x + 1)^n (Ax + B)$$

where n , A and B are constants to be found.

(Total for Question 1 is 4 marks)

2. A curve C has equation

$$y = x^2 - 2x - 24\sqrt{x}, \quad x > 0.$$

- (a) Find (i) $\frac{dy}{dx}$,

(ii) $\frac{d^2y}{dx^2}$.

(3)

- (b) Verify that C has a stationary point when $x = 4$.

(2)

- (c) Determine the nature of this stationary point, giving a reason for your answer.

(2)

(Total for Question 2 is 7 marks)

3.

$$\frac{1+11x-6x^2}{(x-3)(1-2x)} \equiv A + \frac{B}{(x-3)} + \frac{C}{(1-2x)}.$$

(a) Find the values of the constants A , B and C .

(4)

$$f(x) = \frac{1+11x-6x^2}{(x-3)(1-2x)}, \quad x > 3.$$

(b) Prove that $f(x)$ is a decreasing function.

(3)

(Total for Question 3 is 7 marks)

4.

$$g(x) = 4x^3 + ax^2 + 4x + b, \text{ where } a \text{ and } b \text{ are constants.}$$

Given that $(2x + 1)$ is a factor of $g(x)$ and that the curve with equation $y = g(x)$ has a point of inflection at $x = \frac{1}{6}$,

(a) find the value of a and the value of b .

(5)

(b) Show that there are no stationary points on the curve with equation $y = g(x)$.

(2)

(Total for Question 4 is 7 marks)

5.

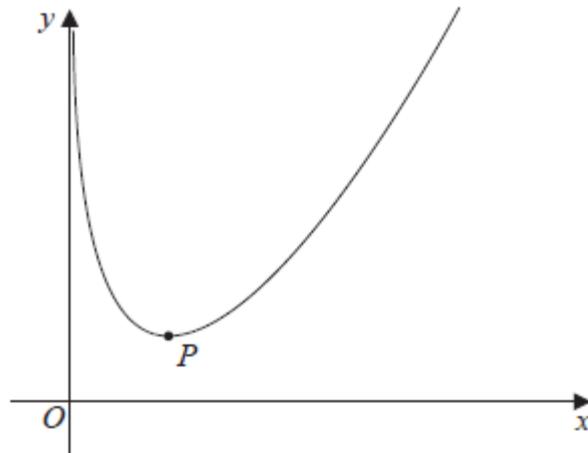


Figure 1

Figure 1 shows a sketch of the curve C with equation

$$y = \frac{4x^2 + x}{2\sqrt{x}} - 4 \ln x \quad x > 0$$

(a) Show that

$$\frac{dy}{dx} = \frac{12x^2 + x - 16\sqrt{x}}{4x\sqrt{x}}$$

(4)

The point P , shown in Figure 1, is the minimum turning point on C .

(b) Show that the x coordinate of P is a solution of

$$x = \left(\frac{4}{3} - \frac{\sqrt{x}}{12} \right)^{\frac{2}{3}}$$

(3)

(Total for Question 5 is 7 marks)

6.

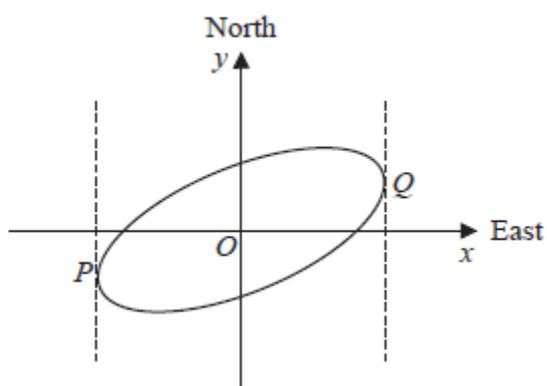


Figure 4

Figure 4 shows a sketch of the curve with equation $x^2 - 2xy + 3y^2 = 50$.

(a) Show that $\frac{dy}{dx} = \frac{y-x}{3y-x}$.

(4)

The curve is used to model the shape of a cycle track with both x and y measured in km.

The points P and Q represent points that are furthest west and furthest east of the origin O , as shown in Figure 4.

Using part (a),

(b) find the exact coordinates of the point P .

(5)

(c) Explain briefly how to find the coordinates of the point that is furthest north of the origin O . (You **do not** need to carry out this calculation).

(1)

(Total for Question 6 is 10 marks)

7. A company decides to manufacture a soft drinks can with a capacity of 500 ml.

The company models the can in the shape of a right circular cylinder with radius r cm and height h cm. In the model they assume that the can is made from a metal of negligible thickness.

- (a) Prove that the total surface area, S cm², of the can is given by

$$S = 2\pi r^2 + \frac{1000}{r} \quad (3)$$

Given that r can vary,

- (b) find the dimensions of a can that has minimum surface area. (5)

- (c) With reference to the shape of the can, suggest a reason why the company may choose not to manufacture a can with minimum surface area. (1)

(Total for Question 7 is 9 marks)

8.

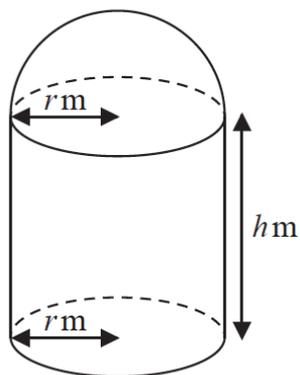


Figure 9

[A sphere of radius r has volume $\frac{4}{3}\pi r^3$ and surface area $4\pi r^2$]

A manufacturer produces a storage tank.

The tank is modelled in the shape of a hollow circular cylinder closed at one end with a hemispherical shell at the other end as shown in Figure 9.

The walls of the tank are assumed to have negligible thickness.

The cylinder has radius r metres and height h metres and the hemisphere has radius r metres.

The volume of the tank is 6 m^3 .

(a) Show that, according to the model, the surface area of the tank, in m^2 , is given by

$$\frac{12}{r} + \frac{5}{3}\pi r^2 \quad (4)$$

The manufacturer needs to minimise the surface area of the tank.

(b) Use calculus to find the radius of the tank for which the surface area is a minimum. (4)

(c) Calculate the minimum surface area of the tank, giving your answer to the nearest integer. (2)

(Total for Question 8 is 10 marks)
